## Scilab: Linear Algebra Quick Reference

## Matrix and Vector Components

| $A=[12 ; 34]$ | Matrix definition |
| :---: | :---: |
| A(i, j) | Entry in row $i$, column $j$ |
| A(i,:) | Row $i$ as vector |
| A( $:, j$ ) | Column $j$ as vector |
| diag(A) | Diagonal entries as vector |
| A(r_1:r_2,c_1:c_2) | Submatrix |
| tril(A) | Lower triangular part of matrix |
| triu(A) | Upper triangular part of matrix |
| $\mathrm{v}=\left[\begin{array}{lll}1 & 2 & 3\end{array}\right]$ | Row vector definition |
| $\mathrm{v}=[1 ; 2 ; 3]$ | Column vector definition |
| v (i) | $i$ th entry in $v$ |

## Matrix and Vector Operations

| A, | Transpose |
| :--- | :--- |
| $\mathrm{A}+\mathrm{B}$ | Sum of matrices |
| $\mathrm{A} * \mathrm{~B}$ | Product of matrices |
| A.*B | Component-wise product of matrices |
| A.*.B | Kronecker product of matrices |
| $\mathrm{A} * * \mathrm{n}$ | Matrix power $A^{n}$ |
| $\operatorname{sum}(\mathrm{v} \cdot * \mathrm{~W})$ | Dot product of $v$ and $w$ |
| $\operatorname{cross}(\mathrm{v}, \mathrm{w})$ | Cross product of $v$ and $w$ |

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## Special Matrices

| $\operatorname{eye}(\mathrm{n}, \mathrm{n})$ | $n \times n$ identity matrix |
| :--- | :--- |
| $\operatorname{zeros}(\mathrm{m}, \mathrm{n})$ | $m \times n$ zero matrix |
| $\operatorname{ones}(\mathrm{m}, \mathrm{n})$ | $m \times n$ matrix with all entries 1 |
| $\operatorname{rand}(\mathrm{~m}, \mathrm{n})$ | $m \times n$ random matrix |
| $\operatorname{diag}([1,2,3])$ | Diagonal matrix |
| $\operatorname{linspace}(\mathrm{s}, \mathrm{e}, \mathrm{i})$ | Vector beginning at $s$, ending at $e$, with $i$ <br> equally distant entries |

## Matrix Propertias

| $\operatorname{rref}(A)$ | Reduced echelon form of $A$ |
| :--- | :--- |
| $\operatorname{det}(A)$ | Determinant of $A$ |
| $\operatorname{inv}(A)$ | Inverse of $A$ |
| $\operatorname{sqrtm}(A)$ | Square root of $A$ |
| $\operatorname{trace}(A)$ | Race of $A$ |
| $\operatorname{rank}(A)$ | Kernel (nullspace) of $A$ |
| $\operatorname{kernel}(A)$ | Eigenvalues of $A$ |
| $\operatorname{spec}(A)$ | $a$ is matrix of eigenvectors, $b$ is |
| $\left[\begin{array}{ll}\text { b }]=\operatorname{spec}(A) & \text { Dimenal matrix of eigenvalues }\end{array}\right.$ |  |
| $\operatorname{size}(A)$ | Returns true if $A$ is square matrix |
| $\operatorname{issquare(A)}$ | Greatest entry in $A$ |
| $\max (A)$ | Least entry in $A$ |
| $\min (A)$ | Singular values of $A$ |
| $\operatorname{svd}(A)$ | Orthogonal basis of $A$ |
| $\operatorname{crth}(A)$ | Cofactors of $A$ |
| $\operatorname{coffg}(A)$ |  |

## Vector Properties

| $\operatorname{norm}(v)$ | Vector length of $v$ (magnitude) |
| :--- | :--- |
| $\operatorname{length}(v)$ | Dimension of $v$ (number of entries) |
| $\operatorname{sum}(v)$ | Sum of entries in $v$ |
| $\operatorname{prod}(v)$ | Product of entries in $v$ |
| $\max (v)$ | Greatest entry in $v$ |
| $\min (v)$ | Least entry in $v$ |

## Elementary Row Operations

|  | Interchange row $i$ and $j$ |
| :---: | :---: |
| A (i, : $)=\mathrm{c} * \mathrm{~A}(\mathrm{i},:$ ) | Multiply row $i$ by $c$ |
| $A(i,:)=A(i,:)+c * A(j,:)$ | Add $c$ times row $j$ to row $i$ |

## COMPONENTS OF NUMBERS

| $\operatorname{int}(x)$ | Integer part of $x$ |
| :--- | :--- |
| round $(x)$ | Round $x$ to nearest integer |
| floor $(x)$ | $\lfloor x\rfloor$, greatest integer less or equal to $x$ |
| $\operatorname{ceil}(x)$ | $\lceil x\rceil$, smallest integer greater or equal to $x$ |
| $\operatorname{sign}(x)$ | Sign; 1 if $x>0,-1$ if $x<0,0$ if $x=0$ |
| $\operatorname{complex}(a, b)$ | Define complex number $a+b i$ |
| $\operatorname{conj}(x)$ | Complex conjugate of $x$ |
| $\operatorname{real}(x)$ | Real part of complex number $x$ |
| $\operatorname{imag}(x)$ | Imaginary part of complex number $x$ |
| fix $(A)$ | Matrix $A$ with all entries rounded down |

## POLYNOMIALS

| $\operatorname{poly}\left(\left[\begin{array}{lll}1 & 2 & 3\end{array}\right], '^{\prime} X^{\prime},{ }^{\prime} C^{\prime}\right)$ | Polynomial $3 x^{2}+2 x+1$ |
| :--- | :--- |
| $\left.\operatorname{poly}\left(\begin{array}{lll}1 & 2 & 3\end{array}\right], X^{\prime} X^{\prime}, r^{\prime}\right)$ | Polynomial in $x$ with roots $1,2,3$ |
| $\operatorname{poly}\left(\operatorname{spec}(A),{ }^{\prime} X^{\prime}, r^{\prime}\right)$ | Characteristic polynomial of $A$ |
| $\operatorname{roots}(p)$ | Roots of polynomial $p$ |

## MATRIX DECOMPOSItIon

| [L U] $=\operatorname{lu}(\mathrm{A})$ | $U$ upper triangular, $A=L U$ |
| :---: | :---: |
| [L U E] = lu(A) | $U$ upper triangular, $L$ lower triangular, $E$ permutation matrix, $E A=L U$ |
| $[\mathrm{Q} R]=\mathrm{qr}(\mathrm{A})$ | $Q$ orthogonal, $R$ upper triangular, $A=Q R$ |
| [Q R E] = $\mathrm{qr}(\mathrm{A})$ | $Q$ orthogonal, $R$ upper triangular, $E$ permutation matrix, $A E=Q R$ |
| [U S V] $=\operatorname{svd}(\mathrm{A})$ | $S$ diagonal, $U, V$ unitary, $A=U S V^{T}$ |

## Components of Numbers

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| $\operatorname{round}(\mathrm{x})$ | Round $x$ to nearest integer |
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